

$$\int \frac{dx}{\sqrt{1+e^x}} = \int \frac{2t dt}{t(t^2-1)} = 2 \int \frac{dt}{t^2-1} = \ln \left| \frac{t-1}{t+1} \right| + C = \ln \left| \frac{\sqrt{e^x+1}-1}{\sqrt{e^x+1}+1} \right| + C.$$

ИНТЕГРАЛЬНОЕ ИСЧИСЛЕНИЕ

积分学

$$\int \frac{dx}{\sqrt{1-x^2}} = \arcsin x + C, \quad \int x^a dx = \frac{x^{a+1}}{a+1} + C, \quad (a \neq -1), \quad \int \frac{dx}{x} = \ln|x| + C.$$

$$\int \frac{dx}{\sqrt{x^2 \pm b}} = \ln \left| x + \sqrt{x^2 \pm b} \right| + C.$$

$$\int \sin^{\frac{3}{4}} x \cos x dx = \int \sin^{\frac{3}{4}} x d(\sin x) = \frac{4}{7} \sin^{\frac{7}{4}} x + C.$$